

Multi-mode measurements in flow ducts and applications

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BACKGROUND









BACKGROUND



No free-field! Most fluid- or turbomachinery problems correspond to confined flows in pipe or duct systems...





Aeroacoustics - Started around 1950's related to noise issues with the then new jet powered civil aircrafts...



$$\frac{1}{c_0^2} \frac{\partial^2 p'}{\partial t^2} - \nabla^2 p' = s$$

Lighthills acoustic analogy



Sir Michael JAMES Lighthill FRS (1924-1998)





Limitations in Lighthill's theory





Alt. 1: Sound production by a flow.

Alt. 2: Sound-vortex interaction (dissipation/ amplification).

Alt. 3: Whistling (Non-linear Aero-Acoustics)



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Limitations in Lighthill's theory





Lighthill or linear Aero-Acoustics is OK

Alt. 1: Sound production by a flow.

Alt. 2: Sound-vortex interaction (dissipation/ amplification).

Alt. 3: Whistling (Non-linear Aero-Acoustics)

• In the low frequency (plane wave) range ($f < f_{cut-on}$) a source is strongly coupled to a system and the acoustic output (power) can vary strongly.



• In the mid frequency range up to $(2-3)x f_{cut-on}$, plane + non-plane waves exist. Also in this range strong coupling between source and system is possible.

• In the high frequency range $f >> 3xf_{cut-on}$, sound propagates as rays, there is no coupling between a source and a system and the acoustic power equals the free field value.

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Coupled models required

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The sound field in a duct can be expanded in propagating waves or modes:



$$\hat{p}(x, y, z) = \sum_{n=0}^{N-1} \left(\hat{p}_{+n} \Psi_n(x, y) \exp(-ik_{+z,n} z) + \hat{p}_{-n} \Psi_n(x, y) \exp(ik_{-z,n} z) \right)$$

where N is at least the number of cut-on modes and z the duct axis.

The sound field in a duct can be expanded in propagating waves or modes:



 $\hat{p}($ The eigenmodes can be based on a rigid walled duct and a plug flow forming a complete functional basis. The axial wave-number should include visco-thermal losses as described e.g. by: C Weng, F Bake (2016), Acta Acustica united Acustica 102(6), 1138-1141.

The sound field in a duct can be expanded in propagating waves or modes:



Assuming we sample the field at $M \ge 2N$ points in space we can write:

$$(\hat{p}_m) = [M_{mn}] \begin{pmatrix} (\hat{p}_{+n}) \\ (\hat{p}_{-n}) \end{pmatrix}, \ M_{mn} = \Psi_n(x_m, y_m) \exp(\mp i k_{\pm z, n} z_m)$$

The sound field in a duct can be expanded in propagating waves or modes:



This is the basis for so called **wave decomposition methods**:

$$\mathbf{p} = \mathbf{M} \begin{pmatrix} \mathbf{p}_{+} \\ \mathbf{p}_{-} \end{pmatrix} \Longrightarrow \begin{pmatrix} \mathbf{p}_{+} \\ \mathbf{p}_{-} \end{pmatrix} = \mathbf{M}^{-1} \mathbf{p}$$

The accuracy will depend on the condition number of **M**, i.e., the sampling positions.

• If only plane waves are propagating then N=1 and we get



J. Y. Chung and D. A. Blaser, "Transfer function method of measuring induct acoustic properties. I. Theory," J. Acoust. Soc. Am. 68, 907-913

Example: Circular duct 6 modes

Condition number:
$$\operatorname{cond}(\mathbf{M}) = \|\mathbf{M}\| \cdot \|\mathbf{M}^{-1}\|$$

Weak singularities: $|z_2 - z_1| = l \frac{\lambda_n}{2}$ $\frac{\theta_2}{\theta_1} = \frac{\pi}{m} l$ $l = 1, 2, 3, \ldots$



From Ref. [12] showing the effect of optimization on a configuration of 12 flush mounted microphones.



The Multi-port relates the amplitudes for modes at two (or several) **Reference cross-sections** (a&b).



Assume **linear** and **time-invariant** systems then a multiport in a duct can in (the Fourier domain) be characterized by



where $p_{+/-}$ represent travelling modal pressure amplitudes and **S** is the **scattering matrix** and p^s represents the **source part**.



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The classical ("first") paper suggesting this:

CREMER L. (1971) "The second annual Fairey lecture: The treatment of fans as black boxes", J. Sound Vib., 16, 1-15



Assume linear and time-invariant systems then a multiport in a duct can in (the Fourier domain) be characterized by



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where $p_{+/-}$ represent travelling modal pressure amplitudes and S_0 is the scattering matrix and p^s represents the source part.

- Projecting the pressure field on the acoustic modes will suppress Hydrodynamic pressure fluctuations
- The effects of boundary conditions are eliminated i.e. reflection free source data can be determined
- Complex systems (low & intermediate frequency range) can be broken down into sub-elements each described by a multi-port



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frequency

Fan measurements as part of the IdealVent project

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- The effect approach is restricted to the ated i.e. reflection f low- and mid-frequency
- Complex s range or (say) 10 modes range) can be broken down into sub-elements each described by a multi-port



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$$\begin{bmatrix} \mathbf{p}_{0+} \ \mathbf{p}_{2+} \dots \mathbf{p}_{(N-1)+} \end{bmatrix} = \mathbf{S} \begin{bmatrix} \mathbf{p}_{0-} \ \mathbf{p}_{2-} \dots \mathbf{p}_{(N-1)-} \end{bmatrix}$$

where the pressure data should be correlated with the external source to supress $p_{+}^{\scriptscriptstyle \mathcal{S}}$

2. Once ${f S}$ is known the source strength can be directly determined from

$$\mathbf{p}_{s+} = \mathbf{p}_{+} - \mathbf{S}\mathbf{p}_{-}$$

3. This is used to estimate the source cross-spectrum matrix

$$\mathbf{G}_{ss} = E\left[\mathbf{p}_{s+}\mathbf{p}_{s+}^{c}\right]$$

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, c stands for the Hermitian.

4. For low Mach-cases the determination of the source data will suffer from bad "S/N" ratios. To improve this correlation based on sets (k) with >=2N samples in each are used

$$\mathbf{p}_{s+} = \mathbf{T}_k \mathbf{p}_{s+,k}$$

where T is a transfer-matrix moving the data to the reference cross-sections (a & b). [13,15]

5. For experimental determination one is limited by the number of pressure probes. A solution is then to measure the reflection matrix **R** for the test rig which leads to

$$\mathbf{p}_{s+} = (\mathbf{E} - \mathbf{S}\mathbf{R})\mathbf{p}_{+} = \underbrace{(\mathbf{E} - \mathbf{S}\mathbf{R})(\mathbf{E} + \mathbf{R})^{-1}}_{C}\mathbf{p}$$

This formulation only requires sets with >= N data points on each side.

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This formulation only requires sets with $\geq N$ data points on each side compared to $\geq 2N$ for alt. 4. [2,3,5,14]

COMPARISON EXPERIMENTAL versus NUMERICAL CHARACTERIZATION

- 1. In **experiments** only **pressure data at the walls** are normally possible to measure.
- 2. In simulations all points can be used AND also all fields are known. This means wave decomposition can be based on pressure and e.g. axial velocity.
- 3. In **experiments** only **wall mounted sources** are normally used to determine the scattering, which makes excitation of single modes difficult. In **simulations** excitation of **single incident modes** is no problem.
- 4. In experiments a low S/N in source strength data can be handled by using a long measurement time. For simulations normally only a short time record is possible (~1 s). BUT a very large number of sampling points are available.

Examples of numerical MULTI-PORT WORKS at KTH



Single Orifice – i) Linearized Navier Stokes Equations (LNSE) – 2-port Scattering matrix & Whistling analysis;
ii) LES – Complete 2-port. [8-10]



T-junction – LNSE model 3-port Scattering matrix-Sound amplification. [11]



Tandem orifice configuration – Complete multi-port up to the radial mode (=6 modes); *Hybrid model* – Scattering using LNSE, Sound generation using hybrid RANS&LES (IDDES). [14,15]



Axial compressor – Modal Source spectra using IDDES. [13]

APPLICATION EXAMPLES-Experiments



• Automotive turbo-charger [6,7]



• Axial fan (IDEALVENT) [13]



• Tandem orifice (IDEALVENT) [14,15]



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CCGEx

ROYAL INSTITUTE OF TECHNOLOGY

Competence Center for Gas Exchange (CCGEx) www.ccgex.kth.se

- Research focus on the gas management of IC engines.
- Combined effort between KTH, the Swedish Energy Agency and some leading OEMs.
- Main research fields are fluid mechanics and acoustics.













Compressor used in experiments

- Passenger car turbo-charger
 Garrett GT1752 driven by the compressed air feed to the turbine.
- Inlet diam. is 44mm.
- Outlet diam. is 42mm.
- The rotor has 6 (+6 splitter) blades.
- Shaft frequency ~80...180kRPM blade pass frequency 8...18kHz.





Acoustic 2-port formulation





• The acoustical performance of a flow duct element is determined by the full 2-port model which consists both the passive and the active parts.



Reflection-free sound generation



 $\boldsymbol{p}^s_+ = (\boldsymbol{E} - \boldsymbol{S}\boldsymbol{R})(\boldsymbol{E} + \boldsymbol{R})^{-1}\boldsymbol{p}$

$$\boldsymbol{G^{s}} = \boldsymbol{p_{s}}(\boldsymbol{p_{s}'})^{\dagger} = \begin{bmatrix} G_{p_{a}^{s}p_{a}^{s}} & G_{p_{b}^{s}p_{a}^{s}} \\ G_{p_{a}^{s}p_{b}^{s}} & G_{p_{b}^{s}p_{b}^{s}} \end{bmatrix}$$



Sound generation of the compressor [7]

- The following can be observed while operating close to deep surge:
 - a large (up to 25dB) broadband increase of SPL;
 - an additional generation of sound at ~.5 of shaft rotating order.





Outlet Sound Generation at 100 000 RPM





Aero-acoustic coupling [7]

- From the S-matrix dissipation (-) or amplification (+) of the compressor can be computed.
- The data shows that approaching surge amplifying flow instabilities, e.g., at ~0.5 RO occur. But the overall losses still dominate.
- The only possibility for a self sustained oscillation ("strong surge") is below 100 Hz.









AIRCRAFT CLIMATE CONTROL SYSTEMS





Overview of results (exp&num) in the project involving KTH

- Analysis (IDDES=RANS+LES) of an axial Liebherr fan unit for aircraft climate systems [13]
- Analysis of single and double diaphragms (orifices) [14,15]
- Novel noise control concepts involving Micro-Perforated-Plates (MPP:s)



Installation effects are an important aspect of the project



Note there are two types: Acoustic and Aerodynamic.

- The Acoustic means the the acoustic nearfields (= noncut on modes) must have decayed at the next element.
- The Aerodynamic means that the inflow to the next element should be back to a "normal" straight pipe condition, i.e., the flow near-fields should have decayed.





Test rig built by VKI & KTH





Axial compressor spectrum [13]

- Axial compressor with strong BPF (2700 Hz) and higher order mode conten
- The (0,0) & (2,0)
- modes are
- particularly strong







Orifice-plate in a circular duct



Active part computed by IDDES and the passive by Linearized Navier Stokes Eqs. (LNSE).

BUT here we will only present the experimental part.







Investigating the **effect of installation (acoustic & aerodynamic)** on the **acoustic properties** of induct orifice plates (separation 2D, 4D and 10D)

The problem is simplified to a single (<u>clean</u>) orifice and a tandem – orifice configuration







The problem is split into sub problems



The installation effects will simply be the difference between 'predicted' and 'real'.

The **Scattering Matrices** will "handle" the acoustic installation effects **BUT** the multiport **Source strength** assumes an undisturbed inflow....

Orifice Measurements



Measurements for model-validation at the Marcus Wallenberg Laboratory for Sound and Vibration Research at KTH



- **2x12 microphones** and **16 loudspeakers** in an optimised setup (max 6 modes)
- Aluminum pipe-sections with constraint layer damping
- Multi-channel excitation with algorithms for simultaneous, uncorrelated excitation
- Modal decomposition with advanced
 wave-numbers to account for damping
- Two stage measurements for accurate
 scattering and source characterisation

Orifice Measurements



Measurements for model-validation at the Marcus Wallenberg Laboratory for Sound and Vibration Research at KTH



Tandem Orifice - Scattering

→ <u>computational inexpensive</u>

Combining two multi-ports is a **multiplication** of their **transfer matrices** Computing the **transfer matrix** is a **linear operation** on the scattering matrix



2D distance

The scattering of an orifice plate is very little affected by disturbed inflow. Even for the shortest separation the Tandem case can be predicted using the Single orifice data.





Tandem Orifice - Source strength

For the source, the power **cross spectrum is computed**, **neglecting correlated sound sources** between the two multi-ports



SUMMARY AND CONCLUSIONS

- The full multi-port approach gives a complete characterization of a duct element (scattering + sound generation)
- Applying the multi-port procedure to experimental or numerical data will eliminate the effect of boundaries i.e. represent the system under reflection free conditions
- The projection of pressure data on acoustic modes i.e. the basis of the modal decomposition used in the process will reduce the influence of hydro-dynamic disturbances ("turbulence")
- Multi-port models have traditionally been applied to fluid machines, e.g., IC-engines and fans and the data (passive/active) determined experimentally

SUMMARY AND CONCLUSIONS

- The low frequency plane wave or 2-port case is today established in particular for the passive part
- In the IDEALVENT project the experimental procedures to determine multi-port data have been further developed
- In addition the usefulness of applying the same procedures on numerical data have been demonstrated for a number of cases



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