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# ASSESSMENT OF TURBULENT PREMIXED COMBUSTION MODELS FOR $CH_4/H_2/AIR$ FLAMES

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This paper presents a comparison of turbulent flame speed based combustion models for  $CH_4/H_2/air$  premixed flames including stretch and heat loss effects. It investigates different reaction rate closure expressions in RANS simulations coupled with a turbulent flame speed model recently proposed by the authors. Heat loss and stretch effects are modelled through the tabulation of laminar consumption speeds in a fresh-to-burnt counter flow configuration with detailed chemistry at various heat loss and flame stretch values. Tabulated values are introduced into the models through the turbulent flame speed expression. The performance of each approach is assessed by comparison with OH<sup>\*</sup> Chemiluminescence images and axial OH<sup>\*</sup> intensity distributions measured experimentally for atmospheric turbulent premixed bluff-body stabilized  $CH_4/H_2/air$  flames ranging from pure methane to pure hydrogen.

Keywords: turbulent premixed combustion, hydrogen enrichment, flame stretch, heat losses, counter flow flames

## 1. Introduction

Conventional premixed combustion modelling approaches have mainly been developed for fuels like CH<sub>4</sub> or natural gas having unity Lewis number (*Le*) and may lead to inaccurate results [1] when used for H<sub>2</sub> or H<sub>2</sub> blended (*Le* < 1) fuels. Additionally, reliable modelling requires to consider stretch and heat loss effects in the premixed flame calculations in order to predict the correct flame stabilization [1–4]. In premixed combustion systems, flame stabilization is commonly provided by means of bluff bodies or swirlers. In such configurations, flames stabilize in the inner and outer shear layer zones, and depending on the interplay between heat loss, flame stretch and hydrogen content in the fuel, flames may or may not stabilize in the shear layers producing M-type, V-type or detached-type mean-flame shapes [5,6].

The authors' recent study [1] based on a turbulent flame speed combustion model showed correct prediction of flame stabilization and shape using RANS CFD for atmospheric lean turbulent premixed  $CH_4/H_2/air$  flames. The improved prediction is due to the consideration of stretch and heat loss effects

into the model. In this study, the turbulent flame speed expression proposed in [1] is incorporated into 4 different reaction rate source term modelling closures (gradient based TFC and FSC, and algebraic EBU like) in the progress variable transport equation. The performance of each model is assessed by comparing CFD RANS computations with  $OH^*$  chemiluminescence data from atmospheric bluff body stabilized turbulent lean premixed  $CH_4/H_2/air$  flame experiments ranging from pure methane to pure hydrogen.

The rest of the paper is organised as follows. First, the non-adiabatic and stretched laminar flame speed calculations are presented in section 2.1. The turbulent flame speed model is illustrated in section 2.2. Modelling approaches for the reaction rate source term are described in section 3. The numerical and experimental setups are shown in section 4.1 and 4.2, respectively, as the model results are presented in section 4.3. Finally, conclusions are discussed in section 5.

### 2. Laminar and turbulent flame speed calculations

#### 2.1 Non-adiabatic and stretched laminar consumption speed calculations

Laminar flame calculations are performed in Cantera 2.4.0 [7] with a fresh-to-burnt counter flow flame configuration under non-adiabatic and stretched conditions. The chemical kinetics is modelled using Aramco-Mech 1.3 [8], while species transport is modelled with a multi-component formulation with Soret effect. Different levels of heat loss  $\beta$  are simulated by decreasing the burnt mixture temperature  $T_p$  according to Eq. (1), while keeping the unburnt mixture temperature  $T_u$  constant. Flame stretch is evaluated from the maximum velocity gradient at the unburnt side (Eq. (1)), and raised by gradually increasing the flow velocities of burnt and unburnt jets.

$$\beta = \frac{T_p - T_u}{T_{ad} - T_u} , \quad \kappa = max \left| -\frac{\partial u}{\partial x} \right|$$
(1)

The flame consumption speed is defined by:

$$S_c = \frac{1}{\rho_u \Delta H_c^o Y_f} \int_{-\infty}^{+\infty} \dot{q} \, dx \tag{2}$$

where  $\rho_u$ ,  $\Delta H_c^o$ ,  $Y_f$  and  $\dot{q}$  are the unburnt mixture density, lower heating value, mass fraction of the fuel, and total heat release rate per unit volume, respectively.



Figure 1: Stretched and non-adiabatic laminar consumption speeds at P = 1 atm and  $T_u = 296$  K, for a)  $0\% H_2 + 100\% CH_4$ ,  $\Phi = 0.7$ , b)  $100\% H_2 + 0\% CH_4$ ,  $\Phi = 0.4$  mixtures

Fig. 1 shows the consumption speed  $S_c$  calculated for the same conditions as the experiments presented later in section 4. The dependence of  $S_c$  on  $\kappa$  and  $\beta$  is markedly different between H<sub>2</sub> and CH<sub>4</sub> fuels. For CFD simulations,  $S_c$  look-up tables are created for all the mixtures listed in Table 1 (for brevity 2 of them shown in Fig. 1) with varying  $\beta$  and  $\kappa$  in the limits of 1.0-0.4 and 0-30000 1/s, respectively.

#### 2.2 Turbulent flame speed calculation

The turbulent flame speed model used in this study is given below [1]:

$$S_t = S_c + \frac{0.4}{\sqrt{Le^*}} u'^{0.8} S_c^{0.45} \alpha_u^{-0.25} l_t^{0.25}$$
(3)

where  $S_c$ ,  $Le^*$ , u',  $\alpha_u$  and  $l_t$  refer to the non-adiabatic laminar stretched consumption speed, effective Lewis number, turbulent velocity, unburnt thermal diffusivity and turbulent length scale, respectively. The effective Lewis number  $Le^*$  is calculated for CH<sub>4</sub>/H<sub>2</sub>/air mixtures as proposed in [9]:

$$Le^* = \frac{\alpha}{x_{H_2}D_{H_2} + x_{CH_4}D_{CH_4}}$$
(4)

where,  $x_{H_2}$  and  $x_{CH_4}$  are the mole fractions of species in the fuel,  $D_{H_2}$  and  $D_{CH_4}$  are the binary mass diffusion coefficients with respect to inert N<sub>2</sub> gas, and  $\alpha$  is the thermal diffusivity of the mixture. All the transport properties are evaluated at the temperature corresponding to the maximum heat release rate in the 1D unstretched adiabatic laminar flame calculation.

In RANS computations of turbulent flame, stretch ( $\kappa$ ) and heat loss ( $\beta$ ) are calculated over the computational domain via Eqs. (5) and (6), then depending on their values, consumption speed  $S_c$  is interpolated from the look-up tables.

$$\kappa = \underbrace{\left(\delta_{ij} - n_{\tilde{l}}n_{\tilde{l}}\right)\frac{\partial \tilde{u}_{l}}{\partial x_{j}}}_{\kappa_{mean}} + \underbrace{\Gamma_{\kappa}\left(\frac{u'}{S_{L0}}, \frac{L}{\delta_{L0}}\right)\frac{\varepsilon}{k}\left[\frac{1}{Le}(1.76 + \tanh(Le - 2))\right]}_{\kappa_{turb}}$$
(5)

$$\beta = 1 - \frac{h_u - \tilde{h}}{\tilde{c}Y_f \Delta H_c^0} \tag{6}$$

In Eq. (5),  $\delta_{ij}$  is Kronecker delta and  $\widetilde{n_i n_j}$  is the orientation factor which is calculated as proposed by [10].  $\widetilde{u}_i$  is the Favre averaged velocity component and  $x_j$  is the spatial coordinate.  $\Gamma_K$  is the ITNFS (Intermittent Turbulence Net Flame Stretch) efficiency function, and is calculated following [11,12]. u', L,  $S_{L0}, \delta_{L0}$  are the turbulent velocity, turbulent integral length scale, adiabatic unstretched laminar flame speed and thickness, respectively. k and  $\varepsilon$  are the turbulent kinetic energy and dissipation rate, and Le is volumetric ratio weighted mixture Lewis number which is calculated following [13]. Further details on the evaluation can be found in [1].

#### 3. Turbulent premixed combustion modelling approaches

In the RANS framework, turbulent premixed combustion can be modelled by solving a Favre averaged transport equation for the combustion progress variable  $\tilde{c}$  [14]:

$$\frac{\partial(\bar{\rho}\tilde{c})}{\partial t} + \frac{\partial(\bar{\rho}\tilde{u}_{j}\tilde{c})}{\partial x_{j}} = \frac{\partial}{\partial x_{j}} \left(\bar{\rho}D_{t}\frac{\partial\tilde{c}}{\partial x_{j}}\right) + \bar{\omega}$$
(7)

where  $\rho$ , t,  $u_j$ ,  $x_j$ ,  $D_t$ , and  $\overline{\omega}$  are the density, time, velocity component, spatial direction, turbulent diffusivity (ratio of turbulent kinematic viscosity to turbulent Schmidt number,  $D_t = v_t/Sc_t$ ), and reaction rate source term, respectively. In Eq. (7),  $\overline{\omega}$  term is responsible for the turbulence chemistry interaction and can be modelled as being function of turbulent flame speed  $S_t$ . In the following subsections, the different reaction rate source term models investigated in this paper, are presented.

#### 3.1 ExtH<sub>2</sub>TFC model

Originally, the TFC (Turbulent Flame Speed Closure) model was developed by Zimont et al. and the reaction source term is modelled as [14]:

$$\overline{\dot{\omega}} = \rho_u S_t |\nabla \tilde{c}| \tag{8}$$

where the magnitude of gradient of progress variable  $\tilde{c}$  is calculated by:

$$|\nabla \tilde{c}| = \left\{ \sum_{j=1}^{3} \left( \frac{\partial \tilde{c}}{\partial x_j} \right)^2 \right\}^{0.5}$$
(9)

The only difference between ExtH<sub>2</sub>TFC model and the original TFC model is that  $S_t$  is calculated from Eq. (3), instead of Zimont's original  $S_t$  expression [14]. Eq. (3) was calibrated against lean premixed CH<sub>4</sub>/H<sub>2</sub>/air flames under atmospheric pressure [1], has Lewis number dependency for hydrogen's high diffusivity and takes into account stretch and heat loss effects through the consumption speed  $S_c$ .

#### 3.2 ExtH<sub>2</sub>FSC model

The FSC (Flame Speed Closure) model was developed by Lipatnikov et al. [15] based on Zimont's TFC model [14] to better reproduce the flame brush development. According to this model,  $D_t$  in Eq. (7) is replaced by  $D_{t,t}$  while  $S_t$  in Eq. (8) is replaced by  $S_{t,t}$  as defined below [15]:

$$D_{t,t} = D_t \left[ 1 - \exp\left(-\frac{t_{fd}}{\tau'}\right) \right], \quad S_{t,t} = S_t \left\{ 1 + \frac{\tau'}{t_{fd}} \left[ \exp\left(-\frac{t_{fd}}{\tau'}\right) - 1 \right] \right\}^{0.5}$$
(10)

The flame development time  $t_{fd}$  and the fully developed flame time scale  $\tau'$  terms, used in Eq. (10), are defined as:

$$t_{fd} = \frac{x_c - x_{fh}}{u_{dump}} , \quad \tau' = \frac{D_t}{u'^2}$$
 (11)

where  $x_c$  is the axial coordinate of the cell of interest,  $x_{fh}$  is the axial coordinate of the flame holder (bluff body top surface in Fig. 2 a), and  $u_{dump}$  is the axial mean velocity at the dump plane.

#### 3.3 ExtH<sub>2</sub>KPP model

The ExtH<sub>2</sub>KPP model is derived from the Schmid model [16]. In his study, Schmid first focused on deriving an analytical expression for the turbulent flame speed  $S_t$ , and then applied KPP (Kolmogorov-Petrovski-Piskunov) theory [12] to derive the following expression for the reaction source term  $\overline{\dot{\omega}}$ :

$$\overline{\dot{\omega}} = C\rho_u \frac{S_t^2}{u'^2 k} \tilde{c}(1-\tilde{c})$$
(12)

In Eq. (12), differently from [16], the turbulent flame speed  $S_t$  of Eq. (3) is utilized and the model constant was calibrated to best match the flame length of the mixture with 56.6% H<sub>2</sub> + 43.4% CH<sub>4</sub> in section 4, resulting in C = 2.5.

#### 3.4 ExtH<sub>2</sub>LV model

In the limit of infinitely thin premixed flames under the flamelet assumption, the reaction rate source term is assumed to have relation  $\overline{\omega} \equiv \rho_u S_t |\nabla \tilde{c}| \equiv \rho_u \langle S_c \rangle \Sigma$  [17]. Assuming an average flame consumption speed  $\langle S_c \rangle \approx S_{L0}$ , and modelling the flame surface density  $\Sigma$  from fractal theories [12,18], Lindstedt and Vaos derived the following closure:

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$$\overline{\dot{\omega}} = C_R \rho_u \frac{S_{L0}}{V_K} \frac{\varepsilon}{k} \tilde{c} (1 - \tilde{c})$$
(13)

In Eq. (13),  $C_R$  is a model coefficient,  $S_{L0}$  is the unstretched adiabatic laminar flame speed,  $V_K$  is the Kolmogorov velocity scale  $V_K = (\varepsilon v)^{0.25}$ , and v,  $\varepsilon$  and k are the molecular kinematic viscosity, turbulence dissipation rate and turbulent kinetic energy respectively. Muppala et al. [19] calibrated the model coefficient as  $C_R = 4.0/e^{Le^*-1}$ , and obtained results in agreement with experimental data for adiabatic premixed CH<sub>4</sub>/H<sub>2</sub>/air flames. In this study, it is proposed to replace  $C_R S_{L0}$  by  $S_t$  (Eq. (3)) obtaining the following reaction rate source term (labelled "ExtH<sub>2</sub>LV model"):

$$\overline{\dot{\omega}} = \rho_u \frac{S_t}{V_K} \frac{\varepsilon}{k} \tilde{c} (1 - \tilde{c}) \tag{14}$$

#### 4. Experimental and CFD results

#### 4.1 Experimental setup

Figure 2 a) shows the experimental setup. The combustor has been operated with 5 different mixtures of CH<sub>4</sub>/H<sub>2</sub>/air premixed gas, ranging from pure methane to pure hydrogen (see Table 1). Air and fuel are mixed a meter before the plenum entrance in order to provide the fully premixed condition at room temperature. The flame is stabilized by a bluff-body supported by a centre rod, producing a blockage ratio of 47%. Images of OH<sup>\*</sup> Chemiluminescence were captured using a Phantom V2012 (LaVision IRO) camera, with a Cerco 2178 UV 100F/2.8 lens equipped with  $310 \pm 10$  nanometer band pass filter. The planar view was obtained using a 3 point Abel deconvolution. Further information on the experimental set-up are available in [5].



Figure 2: Single sector atmospheric test rig schematical view (measurements are in mm)

#### 4.2 CFD calculations

CFD studies were carried out in Ansys Fluent 2019 R3 on the 3D geometry. The progress variable  $\tilde{c}$  equation (Eq. (7)) was solved using the non-adiabatic partially premixed combustion setup with chemical equilibrium chemistry model. Since the cases are perfectly premixed, equations of mixture fraction and its variance were disabled in the solution process. Reynolds stress turbulence model was chosen and the combustion models were introduced via user defined functions (UDFs). Velocity inlet and pressure outlet boundary conditions were applied with the values listed in Table 1. For combustion chamber dump plane and side surfaces (BC 7 and BC 8 in Fig. 2b), shell conduction wall BC is assigned with the wall thicknesses and heat transfer coefficients (HTC) stated in Table 1 with ambient temperature of 296 K. Bluff body (CZC 2 in Fig. 2 b)) is modelled as a solid domain and thermal coupled wall BC is applied. Further information on the computational setup is available in [1].

P[kW]	$V_{H_2}[\%]$	$\Phi[-]$	$u_{in}[m/s]$	$P_{out}[Pa]$	$T_{in}[K]$	BC 7 wall BC	BC 8 wall BC
7	0	0.7	11.8	101325	296	t=10mm, HTC=8.6 W/m <sup>2</sup> K	t=3mm, HTC=150 W/m <sup>2</sup> K
7	25.2	0.7	11.8	101325	296	t=10mm, HTC=8.6 W/m <sup>2</sup> K	t=3mm, HTC=150 W/m <sup>2</sup> K
7	56.6	0.7	11.5	101325	296	t=10mm, HTC=8.6 W/m <sup>2</sup> K	t=3mm, HTC=150 W/m <sup>2</sup> K
7	67	0.7	11.4	101325	296	t=10mm, HTC=8.6 W/m <sup>2</sup> K	t=3mm, HTC=150 W/m <sup>2</sup> K
7	100	0.4	17.1	101325	296	t=10mm, HTC=8.6 W/m <sup>2</sup> K	t=3mm, HTC=150 W/m <sup>2</sup> K

Table 1: Experiment and numerical model conditions

#### 4.3 Reactive flow results

In Fig. 3, the heat release rate (HRR) contours in the mid-section plane obtained from the CFD computations are compared to the experimentally measured normalized Abel deconvoluted OH<sup>\*</sup> chemiluminescence contours. Axial HRR distributions (Fig. 4) are plotted considering that the integral of the distributions from the CFDs should be equal to those from experiments.

As observed from Fig. 3, all models (except ExtH<sub>2</sub>KPP at 25.2% H<sub>2</sub>) could correctly capture the mean flame shape and transition from V flame to M flame (between 0% H<sub>2</sub> and 56.6% H<sub>2</sub>) for all the cases. This shows that the proposed  $S_t$  expression, Eq. (3), works well for these experiment conditions. For the 25.2% H<sub>2</sub> case with ExtH<sub>2</sub>KPP model, the flame could not stabilize, due to a low value of the calibration coefficient *C* in Eq. (13).

ExtH<sub>2</sub>TFC and ExtH<sub>2</sub>FSC models predict almost identical flame stabilization shapes, demonstrating that for the cases investigated in this paper the flame brush development terms described in section 3.2 [15] do not significantly affect the predicted HRR distribution. Due to the gradient dependency  $|\nabla \tilde{c}|$  in the closure, the ExtH<sub>2</sub>TFC and ExtH<sub>2</sub>FSC models, predict thinner flame brush thicknesses than observed in the experiments. Instead, the ExtH<sub>2</sub>KPP and ExtH<sub>2</sub>LV models predict flame brush thickness distribution closer to the experiments due to the  $\tilde{c}(1 - \tilde{c})$  terms. Additionally, ExtH<sub>2</sub>TFC and ExtH<sub>2</sub>FSC models predict almost zero heat release at the flame tip and maximum heat release at the flame attaching points at the wall.

Although all the models show stronger quenching than the experiments at the outer shear layers, the ExtH<sub>2</sub>KPP model predicts even stronger flame quenching than all the other models. This is due to different dependence of ExtH<sub>2</sub>KPP reaction source term on consumption speed (which is responsible for the modelling of quenching effects) compared to the other models: for ExtH<sub>2</sub>KPP  $\overline{\omega} \propto S_c^{0.9}$ , while for the other models  $\overline{\omega} \propto S_c^{0.45}$ .

The best agreements with experiments were achieved with the ExtH<sub>2</sub>LV model in both qualitative and quantitative comparisons by means of mean flame shapes (Fig. 3) and axial HRR distributions (Fig. 4).

## 5. Conclusion

This study investigated a recently proposed turbulent flame speed expression into different reaction rate closure models for CH<sub>4</sub>/H<sub>2</sub>/air flames in RANS context. The performance of four reaction rate closure models was assessed against experimental measurements of premixed bluff body stabilized flames ranging from pure methane to pure hydrogen. From the comparison, four main conclusions were drawn. First, the  $S_t$  expression of Eq. (3) is able to reproduce the transition from M to V flame shapes for increasing hydrogen content for all the investigated closure models, except for the ExtH<sub>2</sub>KPP. Second, closure models based on the algebraic expression  $\tilde{c}(1 - \tilde{c})$  better predicts the flame brush thickness compared to models based on the gradient  $|\nabla \tilde{c}|$  expression. The flame brush development terms in the ExtH<sub>2</sub>FSC model do not appreciably affect the calculated HRR distribution. Third, all the models show stronger quenching in the outer shear layer compared to the experiments. Finally, among the models tested, the best match with the experimental data is obtained by the ExtH<sub>2</sub>LV model.



Figure 3: Abel deconvoluted norm. OH\* chemiluminesence vs norm. heat release rate comparison contours



Figure 4: Normalized axial heat release rate distributions

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